

Binuclear Atoms: a model to explain Low Energy Nuclear Reactions

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(Dated: December 16, 2016)

Abstract

In this paper we show that Helium-like Hydrogen spectra obtained by Randell L. Mills [1] and Ultra Dense Hydrogen obtained by Holmlid [2] are interpretable as experimental evidences of Binuclear Atoms. The Hydrogen Binuclear Atom, a model proposed 25 years ago, is a metastable configuration in which the two nuclei are held together at a very short distance in an atom-like configuration. This should be a peculiar configuration of the Hydrogen molecule where nuclei are characterized by a high kinetic energy, and nuclear motion is coupled with electronic motion. This is a completely different model from the usual Born-Oppenheimer picture of atoms and molecules we are used to, where nuclei oscillate about their equilibrium positions and electronic motion is decoupled from the nuclear one. The identification of Helium-like Hydrogen Spectra and Ultra Dense Hydrogen as Binuclear Atoms has a strong impact on one of the main objections to Low Energy Nuclear Reactions (LENR): the overcoming of the Coulomb barrier thus identifying a sound mechanism for the occurrence of LENR.

Far from being conclusive, this work has the only aim to take this hypothesis more seriously, and focus the attention of people interested in LENR mechanism on this subject.

INTRODUCTION

One of the major objections to Low Energy Nuclear Reactions is the lacking of a model able to explain the possibility for two nuclei to be at a short distance for a time sufficiently long to trigger nuclear reactions. The lack of a mechanism for the overcoming of the Coulomb barrier is an argument that dismisses any claim of nuclear reactions. Taking as an example the Rossi-Focardi paper [3] is no exception. Discussing the Nickel-Hydrogen system, trying to evaluate the possibility of nuclear reactions, they calculate the tunneling probability P of the proton getting in close contact with Ni nucleus using the Gamow formula, which in Evans approximation is: [4]

$$P \approx e^{-(2\pi zZ/137\beta)} \quad (1)$$

where z and Z are the charge values for Ni ($Z = 28$) and H and $\beta = \frac{v}{c}$ is the ratio between the velocity of the incoming particle and the velocity of light. Considering that the kinetic energy can be evaluated as $E_c = \frac{1}{2}mv^2 = \frac{3}{2}kT$ where the temperature is about 1000 K, we obtain a kinetic energy of $E_c \approx .13 \text{ eV}$. Putting these values in formula (1) we obtain an exceedingly small probability of tunneling, which is $P \approx e^{-2440} \approx 4.7 \cdot 10^{-1059}$, a value that does not account for the occurrence of nuclear events.

BINUCLEAR ATOMS

In 1991, G. F. Cerofolini [5] put forward a theory to explain some experimental results obtained with ion implantation experiments. In ion implantation experiments, ions are accelerated at various range of energies towards a solid target. This process gives rise to, among others, atom-atom head-on collisions at a broad range of energies, down to the eV range when the projectile has lost most of its initial kinetic energy. We here refer in particular to papers [6] and [7]. In summary, various deuterated targets (as an example *TiD*) are bombarded with clusters of deuterated molecules (as an example D_2O), and deuteron-deuteron fusion rate is measured as a function of the impinging projectiles. The analysis of experimental data takes Cerofolini to the hypothesis of a precursor, a metastable state at about 30 eV, which should be responsible for the high fusion rate measured: the Binuclear Atom.

In an initial formulation, Binuclear Atoms are defined in ref. [8] in the following way:

consider the head-on collision of two atoms with atomic number Z_1 and Z_2 . Particularly interesting is the situation of a kinetic energy sufficient to bring the nuclei to a distance smaller than the radius of the most bound electron. In this case the electrons can rearrange to assume, at least temporarily, a configuration that resembles that of the atom with atomic number $Z_1 + Z_2$, because this configuration has a binding energy much lower than the one of the two separate atoms. Considering only one electron, being the energy for the first orbit of the hydrogen-like atom $E(Z) = Z^2 E_0$ it follows that $E(Z_1 + Z_2) < E(Z_1) + E(Z_2)$. This excess binding energy can partially balance the internuclear Coulomb repulsion and temporarily stabilize the resulting binuclear atom. After some considerations, Cerofolini concludes that the existence of binuclear atoms is limited to a few couples of light atoms [8].

In a second paper [9], Cerofolini writes: *Binuclear atoms are metastable configurations in which two nuclei are held together by the electronic energy of the orbiting electrons in an atomic-like configuration. The hydrogen- hydrogen helium-like binuclear atom $(H+H+)2e^-$ is explicitly predicted to exist, although the activation energy required for its formation (~ 30)eV is extremely high for ordinary chemistry, so that it can only be formed under very special conditions such as the ones occurring inside a dense collisional cascade. The $(H+H+)2e^-$ binuclear atom is predicted to be metastable with a remarkably high activation energy (of several electron volts) for its dissociation. In the $(H+H+)2e^-$ binuclear atom, the electronic energy is not a constant of motion and is coupled with the nuclear kinetic energy, and the nuclei move with a kinetic energy of the order of 10 eV although they remain localized in a region of 0.4 to $0.5a_0$, where a_0 is the Bohr radius ($a_0 = 0.53 \times 10^{-8} \text{cm}$) [9].*

So Cerofolini's idea of Binuclear Hydrogen was a short-lived kind of Hydrogen, where the two protons are trapped at a very short distance and consequently electrons, orbiting in space around a more concentrated positive charge, tended to assume Helium-like character. This was 1992, long before spectroscopic results of a Helium-like Hydrogen spectrum was obtained and brought to the scientific community knowledge.

EXTREME ULTRAVIOLET SPECTROSCOPY OF HELIUM-HYDROGEN PLASMA

Randell L. Mills, in his work *Extreme ultraviolet spectroscopy of helium-hydrogen plasma* [1], is able to show the formation of novel hydrogen emission lines (see figure 1) of a mixture of 98% Helium and 2% Hydrogen plasma at room temperatures and low pressure. The origin

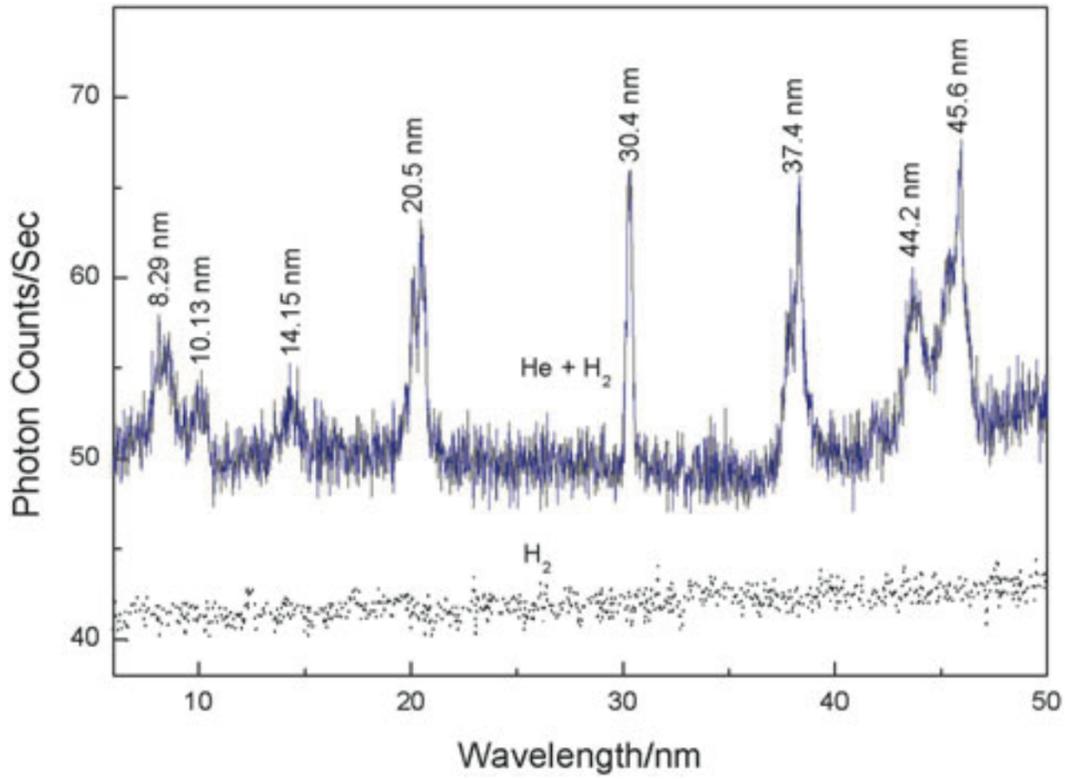


FIG. 1. Figure taken from ref. [1]. The short wavelength EUV spectra (5–50 nm) of the microwave cell emission of the helium–hydrogen mixture (top curve) and control hydrogen (bottom curve).

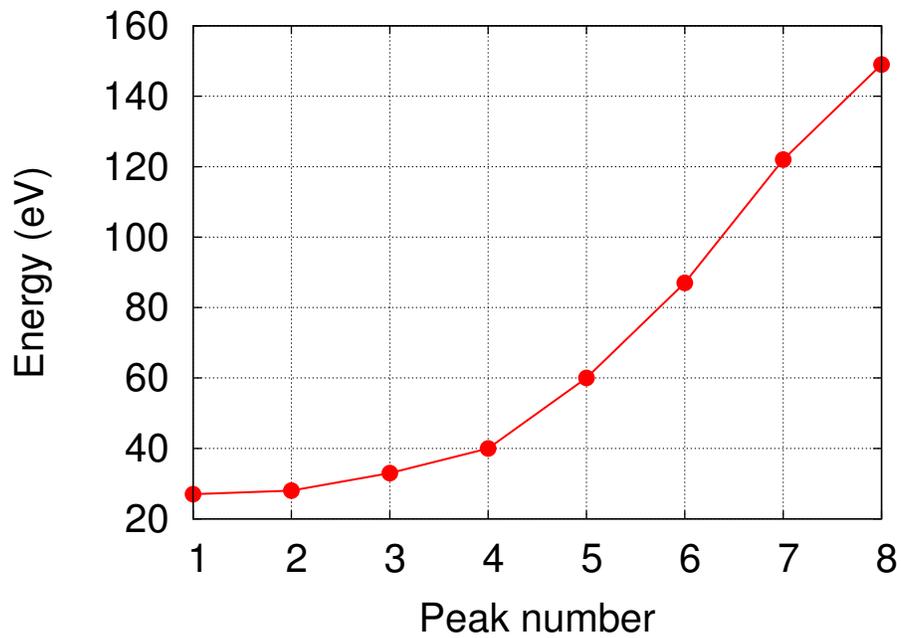


FIG. 2. Energies corresponding to the new Hydrogen peaks in Mills paper [1].

of the new lines cannot be easily determined: trivial explanations based on known chemical species of Helium or Hydrogen compounds are ruled out. The new lines appear only in Helium-Hydrogen mixtures, but not in Helium or Hydrogen alone, and not in mixtures of Hydrogen with other noble gases. Experimental data have been replicated in other laboratories. Although Helium seems not to be responsible for these lines, Hydrogen instead shows an anomalous Doppler broadening in its atomic spectrum but at the same time it's not clear how a species of Hydrogen could bound an electron at an higher energy than the first Bohr energy, which is 13.6 eV , whereas novel emission lines are at energy higher than 27.1 eV . Mills explains new emission lines with a new theory [11], the Hydrino, which should be the new fundamental state of atomic Hydrogen.

Yet we can refute this interpretation thinking of the formation of a Binuclear Hydrogen metastable state. Consider that, due to catalytic action of Helium, Hydrogen binuclear atoms are formed in Helium-Hydrogen plasma. If the two Hydrogen nuclei are close enough, electrons orbiting around them can rearrange taking Helium characteristics, hence the origin of Helium-like Hydrogen spectrum.

Looking more closely to the energy diagram of the new Hydrogen peaks, taken from figure (1), we can appreciate that the diagram formed (see figure 2) is similar to a parabola. Recall that the eigenvalue structure $E \approx n^2$ is characteristic of a particle in a infinite square well. This could indicate that the two protons get trapped in a potential well when their distance $r \rightarrow 0$. Since we are outside the realm of the Born-Oppenheimer approximation, what we see here should be at the same time the electronic and nuclear eigenvalue, because electronic and nuclear motion should be strongly coupled.

Before leaving Mills work, let us add a final important remark which we will recall later. These results have been replicated in different laboratories [10], where it has been observed an anomalous broadening of hydrogen Balmer lines, and according to Mills [1] the average hydrogen atom temperature is $180 - 210\text{ eV}$ versus $\approx 3\text{ eV}$ for pure hydrogen (see figure 3 for details). An abnormal high protonic kinetic energy is a common feature that introduces us to the next experimental result: Ultra Dense Hydrogen.

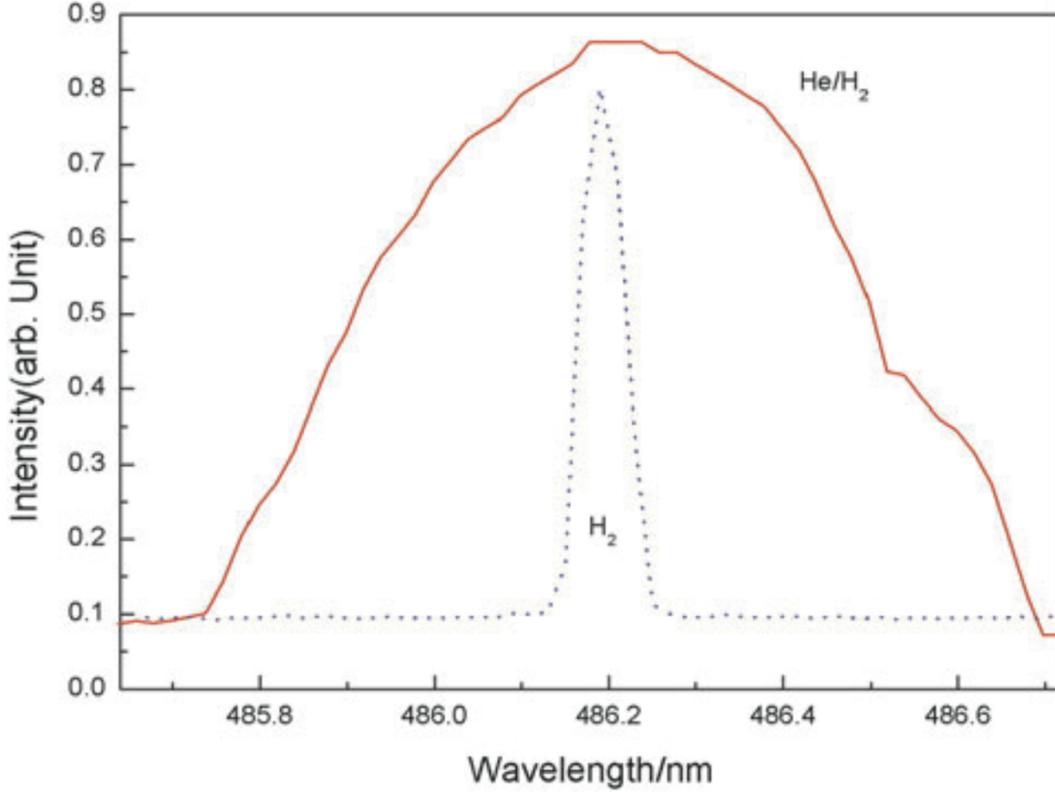


FIG. 3. Figure taken from ref. [1]. The 656.3 nm Balmer α line width recorded with a high resolution (± 0.006 nm) visible spectrometer on helium–hydrogen (90/10%) and hydrogen microwave discharge plasmas. Significant broadening was observed from the helium–hydrogen plasma corresponding to an average hydrogen atom temperature of 180–210 eV compared to ≈ 3 eV for hydrogen alone.

ULTRA DENSE HYDROGEN

Working with Rydberg Matter, Prof. Holmlid is able to obtain in his laboratory a peculiar form of Ultra Dense Hydrogen and Deuterium with the following surprising characteristics: the two nuclei possess a kinetic energy up to 1000 eV and supposedly lie at a distance of the order of 10^{-2} Å [2]. The lower range of energies measured by Holmlid overlaps with the high range of energies found from Mills for Helium-like Hydrogen Spectra. §

Rydberg Matter [12] is a state of matter formed by Rydberg Atoms, which are atoms where the outermost electrons are found in excited planar circular orbits. Planar clusters of these atoms share these peripheral electrons that are loosely bound to the internal core of atoms. Rydberg electrons in the cluster are delocalized in a conduction band as in a metal.

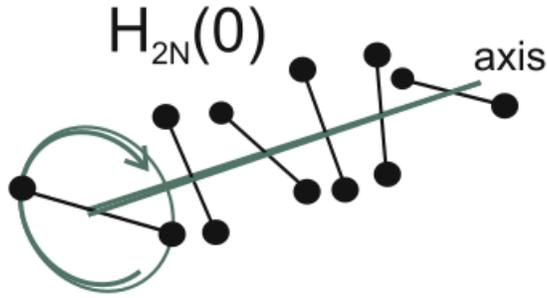


FIG. 4. Ultra Dense Hydrogen structure proposed from Prof. Holmlid – see ref. [2]

Being in this way, normal bound distances in Rydberg Matter are of the order of 10 Å and more. On the contrary, the structure of Ultra Dense Hydrogen or Deuterium appears different from ordinary Rydberg Matter: the main problem is how to cope with the behavior of electrons in this structure. If nuclei are at a such short distance, how could electrons, orbiting in a very large orbit far away from nuclei, screen the nuclei Coulomb repulsion?

Needless to say, Prof. Holmlid proposes for Ultra Dense Hydrogen a different kind of Rydberg Matter based on spin (see figure 4). Anyway, we propose that Ultra Dense Hydrogen is a form of Binuclear Atom, that is able to form thanks to the interaction with the surface of Fe catalyzer used. A very interesting paper explains how a metallic surface can bring two charges of the same polarity to small distance that can be orders of magnitude smaller than the equilibrium separation of the pair potential minimum [13]. Maybe the metallic surface can have a catalytic action in both Rossi and Holmlid environments bringing pair of protons to small distances, where the binuclear atom state may be triggered.

DISCUSSION

Due to the lack of a known analytical form, the solution to the equation for the Hydrogen molecule has to be found numerically. Since 1964, with the work of Kolos and Wolniewicz, the wavefunction is determined solving the Schrödinger equation for the following Hamiltonian without assuming the Born-Oppenheimer approximation, i.e treating protons and electrons on equal footing: [14–19]

$$H_0 = \sum_i \frac{p^2}{2m_i} + \sum_{i>j} \frac{q_i q_j}{r_{ij}} \quad (2)$$

where indices i and j span over all 4 particles, \vec{r}_{ij} is the vector from particle i to particle j . We use atomic units i.e. $q = m_e = \hbar = 1$ and the fine structure constant $\alpha^{-1} = c \approx 137$. A solution of the Schrödinger equation $H_0\psi = E\psi$ is variationally determined that, at this level, does not yet take into account spin, relativistic or QED effects. Being small, these corrections can be handled as a standard procedure using perturbation theory: the corrections are evaluated as expectation value of the Hamiltonian describing the perturbation with the unperturbed wavefunction obtained before. Using this schema, the corrections to the energy determined using H_0 Hamiltonian, may be ordered in terms of powers of the fine structure constant in the following way: [18, 20]

$$E(\alpha) = E^{(0)} + E^{(2)} + E^{(3)} + E^{(4)} \dots \quad (3)$$

Each $E^{(n)}$ contains the correction of the order α^n : $E^{(0)}$ is the eigenvalue of the non relativistic Schrödinger equation, H_0 , whereas $E^{(2)}$ is the expectation value of the Breit-Pauli Hamiltonian, $E^{(3)}$, $E^{(4)}$ and following are the various orders of QED contributions. For the purpose of this work it is sufficient to stop at the Breit-Pauli Hamiltonian level which is composed of several terms:

$$H_{BP} = H_{MV} + H_{DW} + H_{OO} + H_{SO} + H_{SS} \quad (4)$$

where the various components are: H_{MV} is the Mass-Velocity term, H_{DW} is the Darwin term, H_{OO} the Orbit-Orbit interaction, H_{SO} the Spin-Orbit interaction, finally H_{SS} is the Spin-Spin interaction term. For our goal it is sufficient to examine in detail the corrections relative to the two protons only in the case depicted in figure 5. We derive our formulas from a symmetric approach to the Breit-Pauli Hamiltonian as can be found in the following paper [21] considering that for a motion around the common center of mass we have $\vec{p}_1 = -\vec{p}_2$ (see fig 5). Here \vec{r} is the proton-proton distance, m the proton mass, $\vec{\mu} = e g \vec{s} / (2m)$ its magnetic moment. The superscript pp means that this is the correction due to protons only.

$$H_{OO}^{pp} = -\frac{\alpha^2}{4m^2} \frac{\vec{p}_1 \cdot \vec{p}_2}{r} \quad (5)$$

$$H_{SO}^{pp} = -\frac{g\alpha^2}{m^2} \frac{(\vec{s}_1 + \vec{s}_2) \cdot \vec{r} \times \vec{p}_1}{r^3} \quad (6)$$

$$H_{SS}^{pp} = \frac{g^2\alpha^2}{4m^2} \frac{\vec{s}_1 \cdot \vec{s}_2}{r^3} \quad (7)$$

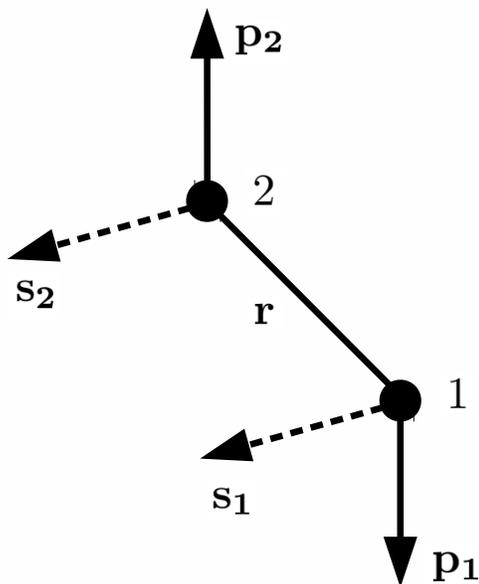


FIG. 5. Two protons rotating around the common center of mass with parallel spin

Obviously these corrections are exceedingly small if compared to the electronic ones due to the proton squared mass at the denominator, which lowers the nuclear contribute by six orders of magnitude.

But what is interesting to observe, and is the core of this paper, is the functional form of these corrections and their behavior compared to the Coulomb repulsion $1/r$ when $r \rightarrow 0$. As we can see, the three expressions H_{OO}^{pp} (5), H_{SO}^{pp} (6), H_{SS}^{pp} (7) are asymptotic to $1/r$, $1/r^2$, $1/r^3$ respectively. So, depending on how spin are mutually oriented, the sign of H_{SO}^{pp} and H_{SS}^{pp} changes consequently. Anyway, for $r \rightarrow 0$ the leading term seems to be H_{SS}^{pp} (7), that, in case of opposite protonic spin goes to $-\infty$ for $r \rightarrow 0$ as $1/r^3$. As we have said, Breit-Pauli Hamiltonian is an expression that has to be used in perturbative way, and as such it represents the first order correction to expression H_0 (2) for nuclear velocity and spin. Consequently, it's not correct to extrapolate system behavior for $r \rightarrow 0$ which is a condition very far from the Born Oppenheimer minimum we are describing through use of H_0 Hamiltonian (2). But if we take the Breit Pauli Hamiltonian as an indication, we may speculate that the energy of the system may somehow lower for $r \rightarrow 0$, thus creating a potential well for the two protons at a smaller distance than the usual Hydrogen bond length. This fact should be investigated with more strong theoretical means such as, for

instance, a suitable version of the Dirac equation.

If such a bound state exists, it should be called "Binuclear Atom" and it should present features similar to Helium-like Hydrogen Spectra and Ultra Dense Hydrogen together. The reason is simple: two protons orbiting very near in space would produce an electric field similar to the one produced by the Helium nucleus. Moreover, because we are not in Born Oppenheimer conditions, the nuclear excited state directly modifies electronic eigenvalues as well, originating high energy lines of the spectrum. As far as Ultra Dense Hydrogen is concerned, we have to recall that a Binuclear Atom should be characterized by the axis of rotation of protons. This anisotropy could be at the same time cause and effect of a magnetic field and, depending on the formation mechanism, it would be possible to find several Binuclear Atoms stacked in columns as proposed by Holmlid (figure 4).

CLOSING REMARKS

We have tried to show that the Binuclear Atom model is able to explain different peculiar experimental results. The existence of helium-like Hydrogen spectra, which occur only in Helium-Hydrogen mixed plasma, points to a formation of a metastable form of Hydrogen characterized by a high protonic kinetic energy and helium-like electronic spectrum. On the other hand, the evidence of Ultra Dense Hydrogen may be interpreted as the formation, through the assistance of a metallic surface, of another metastable Hydrogen characterized by a very short proton-proton distance and a very high kinetic energy.

Last but not least, we can consider the consequences of Ultra Dense Hydrogen in Rossi Ecat. If Nickel lattice surface is able to form Binuclear Atoms, we may recalculate through the Gamow formula the probability that hydrogen gets in contact with Nickel nucleus. Using an energy value for protons of ≈ 1000 eV instead of $\approx 0,13$ eV [2, 3], the calculated probability value becomes $P \approx 10^{-12}$. This is a rather different value than the Rossi and Focardi one, and could account for the occurrence of nuclear reactions.

The Binuclear Atom Model is the missing link between Physics and Chemistry.

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